

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

## **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/42

Paper 4 (Extended)

October/November 2016

MARK SCHEME
Maximum Mark: 120

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## **Abbreviations**

answers which round to awrt correct answer only cao

dep dependent

follow through after error ignore subsequent working FΤ isw

or equivalent Special Case oe SC

not from wrong working seen or implied nfww

soi

Qu	estion	Answer	Mark	Part Marks
1	(a)	171	1	
	(b)	10	1	
	(c)	172	1	
	(d)	4	2	<b>B1</b> for 170 or 174 seen
	(e)	172.1	2	<b>M1</b> for attempt at $\sum fx$ soi by 24099 or 172 or 172.1
2	(a)	2.83 or 2.828	3	<b>B2</b> for $\sqrt{8}$ or $2\sqrt{2}$ final answer or <b>M2</b> for $2^2 + 2^2$ or <b>M1</b> for correct sketch
	(b)	225 cao	2	<b>B1</b> for 45 soi by e.g. 135 If 0 scored <b>SC1</b> for 224.9 to 225.1
	(c)	8 cao	2	<b>M1</b> for $2 \times 3 + 0.5 \times 2 \times 2$ oe
3	(a)	Positive	1	
	(b) (i)	12.15	1	
	(ii)	66	1	
	(c) (i)	y = 37.2 + 2.37x	2	Range 37.20 to 37.21 and 2.369 to 2.370 <b>B1</b> for 37.2 + $kx$ , or $a + 2.37x$ , If 0 scored, <b>SC1</b> for 37 + 2.4 $x$
	(ii)	82 or 82.2	1	FT their (i)

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Qu	estion	Answer	Mark	Part Marks
4	(a)	48	1	
	(b)	84	2	FT $(180 - 2 \times their (a))$ , their $(a) \neq 45$ M1 for $(180 - 2 \times their (a))$ their $(a) \neq 45$
	(c)	42	1	<b>FT</b> <i>their</i> (b) ÷ 2
	(d)	69 cao	2	<b>B1</b> for angle $OBC$ or $OAC = 21$ or angle $ABC = 69$
	(e)	55.5	2	FT their (d) M1 for (180 – their (d)) ÷ 2
5	(a)	36.7 or 36.68 to 36.69	2	<b>B1</b> for at least 3 of (7.5, 17.5, 30, 42.5, 70) soi by 4402.5 Accept 37.2 or 37.18 to 37.19 for full marks and 3 of (8, 18, 30.5, 43, 70.5) soi for <b>B1</b>
	(b)	0.8, 3.6, 2.6, 2.7, 1.47 or 1.466 to 1.467, 0.7	3	B2 for 4 or 5 correct or B1 for 2 or 3 correct
6	(a)	Reflection $y = x$	2	B1 for each
	(b)	Rotation, centre (2, 3) 90 [anticlockwise] or 270 clockwise	2	B1 for each
	(c)	Translation $\begin{pmatrix} -4 \\ 3 \end{pmatrix}$	2	B1 for each
	(d)	Enlargement, centre (0, 0)	2	Allow reduction
		[SF] $\frac{1}{3}$ oe		B1 for each
7		Correctly equating one set of coefficients	M1	Equation $x = \text{or } y = \text{from one equation}$
				Note – a correct sketch showing intersection in third quadrant scores <b>M2</b> (other sketches may score the <b>M1</b> for $y = \dots$ seen)
		Correct method to eliminate one variable	M1	Correct substitution into other equation
		$x = -2$ $y = -\frac{1}{2}$	B2	B1 for each If zero scored SC1 for correct substitution into one of original equations and evaluation to find other variable

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Qu	estion	Answer	Mark	Part Marks
8	(a)	$\frac{\sqrt{8}}{3}$ or $\frac{2\sqrt{2}}{3}$ or $\sqrt{\frac{8}{9}}$	3	M2 for $\frac{\sqrt{3^2 - 1^2}}{3}$ or M1 for $3^2 - 1^2$
				If 0 scored, <b>SC1</b> for 0.943 or 0.9428 or $\sqrt{0.889}$
	(b) (i)	$[\cos B] = \frac{9^2 + 10^2 - 11^2}{2 \times 9 \times 10}$ oe	2	<b>M1</b> for $11^2 = 9^2 + 10^2 - 2 \times 9 \times 10 \times \cos B$
	(ii)	$0.5 \times 9 \times 10 \times their$ exact (a)	M2	M1 for $0.5 \times 9 \times 10 \times their$ (a) (their (a) must be < 1)
		Leading to $30\sqrt{2}$	A1	Cancelling seen or $\frac{180\sqrt{2}}{6}$ or $\frac{90\sqrt{2}}{3}$ or $\frac{60\sqrt{2}}{2}$ seen
9	(a)	21.5 or 21.45 to 21.46	2	<b>M1</b> for $100 - \pi \times 5^2$ oe
	(b) (i)	5.77 or 5.773 to 5.774	2	<b>M1</b> for $\tan 60 = \frac{10}{x}$ oe
	(ii)	21.5 or 21.54 to 21.55	2	M1 for $10 + 2 \times their$ (b)(i) oe or $10 + \frac{10}{\sin 60}$ oe
	(iii)	100 to 101.0 nfww	4	M3 for $0.5 \times 10 \times their$ (b)(i) + $0.5 \times 10 \times their$ (b)(i) + $0.5 \times 10 \times 10 \sin 60$ oe or M2 for any 2 of these or M1 for any 1 of these
				OR
				M3 for $0.5 \times (their(b)(ii))^2 \times \sin 60 - 10^2$ oe or M2 for $0.5 \times (their(b)(ii))^2 \times \sin 60$ oe or M1 for <i>their</i> attempt at area of triangle $ABC - 100$

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Question	n	Answer	Mark	Part Marks
10 (a)		Fully correct curve	3	B2 for both branches but with serious 'curl back' and/or overlap. or B1 for 1 branch
(b)		x = 2 $y = 3$	2	B1 for each
(c)		$\begin{bmatrix} x = ] -4 \\ [x = ] 3 \end{bmatrix}$	2	B1 for each
(d)		$   \begin{array}{l}     x < -4 \\     2 < x < 3   \end{array} $	1 2	FT their –4 from (c) FT their 2 from (b) and their 3 from (c) B1 for each
(e)	(i)	Translation $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$	2	B1 for each
	(ii)	Translation $\begin{pmatrix} 0 \\ 3 \end{pmatrix}$	2	B1 for each
11 (a)		$ \begin{array}{c} 216 \\ n^3 \end{array} $ oe	1 1	
(b)		43 $n^2 + n + 1$ oe	1 3	M2 for $pn^2 + qn + c$ $p, q, c \neq 0$ or M1 for second differences = 2 or $pn^2 + c$ or $pn^2 + qn$
(c)		$173$ $n^3 - n^2 - n - 1$ oe	1 3	FT their (a) – their (b) FT their (a) – their (b) M2 for $pn^3 + qn^2 + rn + c$ $p, q, r, c \neq 0$ or $n^3$ – their (b) or M1 for third differences = 6 or for $pn^3 + qn^2 + c$ or $pn^3 + qn^2 + rn$ or $pn^3 + rn + c$

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Quest	tion	Answer	Mark	Part Marks
12 (a	a) (i)	144π	2	M1 for $\frac{2}{3} \times \pi \times 6^3$
	(ii)	108π	2	M1 for $2\pi \times 6^2 + \pi \times 6^2$ If 0 scored SC1 for $72\pi$
(1	b) (i)	12 or 11.99 to 12.01 nfww	3	M2 for $\frac{their(a)(i)\times 16}{\frac{4}{3}\pi}$ oe
				or <b>M1</b> for $\frac{4}{3} \times \pi \times r^3 = their(a)(i) \times 16$
	(ii)	1:3 or $\frac{1}{3}$ :1 cao nfww	3	<b>M2</b> for $4 \times \pi \times (their(b)(i))^2 : 16 \times their(a)(ii)$ oe or <b>M1</b> for $4 \times \pi \times (their(b)(i))^2$ or $16 \times their(a)(ii)$
13 (a	a)	$\frac{p^3q^2}{6}$ final answer	3	M1 for correct use of $a \log b$ M1 for correct use of $\log a \pm \log b$
(1	b) (i)	1.29 or 1.292	3	<b>M2</b> for $\frac{\log 6}{\log 4}$ or $\log_4 6$ or sketch of $y = 4^x$
				and $y = 6$ oe or M1 for $x \log 4 = \log 6$ or sketch of $y = 4^x$
	(ii)	$6x^2 - 5x - 7 = 0$	B2	or <b>B1</b> for 3 terms correct in expansion $6x^2 - 9x + 4x - 6$
		$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4 \times 6 \times (-7)}}{2 \times 6}$	M1	FT their three term quadratic or for sketch of parabola with minimum point
				Alternative If sketch of parabola with minimum point and $y = 1$ and no three term quadratic seen, allow <b>B3</b>
		x = 1.57  or  1.574 x = -0.741[01]	B2	B1 for each

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Question	Answer	Mark	Part Marks
14 (a)	Fully correct curve  12	4	<b>B1</b> for correct graph for $x < 0$ , minimum point seen above $x$ -axis <b>B1</b> for correct graph for $0 < x < 2$ , maximum point seen higher than minimum point <b>B1</b> for minimum point seen below $x$ -axis, $2 < x < 8$ If 0 or 1 scored, <b>SC2</b> instead for 'correct curve' except stationary point of inflexion instead of LH minimum and maximum
(b)	0.729 or 0.7287 -10.3 or -10.26	2	B1 for each
(c)	(1.31 or 1.311 to 1.312, 1.73[0])	2	B1 for each co-ordinate
(d)	-2.82, 0.364, 4.23, 5.76 or -2.824 to -2.823 0.3643 to 0.3644 4.228 to 4.229 5.758	4	B1 for each If 0 scored SC2 for -2.8, 0.36, 4.2, 5.8 or SC1 for three of these.